

%\begin{abstract}

There are two basic approaches to quantum TGD. The first approach, which is discussed in this chapter, is a generalization of Einstein's geometrization program of physics to an infinite-dimensional context.

Second approach is based on the identification of physics as a generalized number theory. The first approach relies on the vision of quantum physics as infinite-dimensional Kähler geometry for the \blockquote{world of classical worlds} (WCW) identified as the space of 3-surfaces in in certain 8-dimensional space.

There are three separate manners to meet the challenge of constructing WCW Kähler geometry and spinor structure. The first approach relies on direct guess of Kähler function. Second approach relies on the construction of Kähler form and metric utilizing the huge symmetries of the geometry needed to guarantee the mathematical existence of Riemann connection. The third approach relies on the construction of spinor structure based on the hypothesis that complexified WCW gamma matrices are representable as linear combinations of fermionic oscillator operator for second quantized free spinor fields at space-time surface and on the geometrization of super-conformal symmetries in terms of WCW spinor structure.

In this chapter the proposal for Kähler function based on the requirement of 4-dimensional General Coordinate Invariance implying that its definition must assign to a given 3-surface a unique space-time surface. Quantum classical correspondence requires that this surface is a preferred extremal of some some general coordinate invariant action, and so called Kähler action is a unique candidate in this respect. The preferred extremal has in positive energy ontology interpretation as an analog of Bohr orbit so that classical physics becomes and exact part of WCW geometry and therefore also quantum physics. In zero energy ontology (ZEO) it is not clear whether this interpretation can be preserved except for

maxima
of Kähler function.

The basic challenge is the explicit identification of WCW Kähler function \mathcal{K} . Two assumptions lead to the identification of \mathcal{K} as a sum of Chern–Simons type terms associated with the ends of causal diamond and with the light-like wormhole throats at which the signature of the induced metric changes. The first assumption is the weak form of electric magnetic duality. Second assumption is that the Kähler current for preferred extremals satisfies the condition $j_K \wedge dj_K = 0$ implying that the flow parameter of the flow lines of j_K defines a global space-time coordinate. This would mean that the vision about reduction to almost topological QFT would be realized.

Second challenge is the understanding of the space-time correlates of quantum criticality. Electric–magnetic duality helps considerably here.

The realization that the hierarchy of Planck constant realized in terms of coverings of the imbedding space follows from basic quantum TGD leads to a further understanding. The extreme non-linearity of canonical momentum densities as functions of time derivatives of the imbedding space coordinates implies that the correspondence between these two variables is not 1–1 so that it is natural to introduce coverings of $CD \times CP_2$.

This leads also to a precise geometric characterization of the criticality of the preferred extremals. Sub-algebra of conformal symmetries consisting of generators for which conformal weight is integer multiple of given integer n is conjectured to act as critical deformations, that there are n conformal equivalence classes of extremals and that n defines the effective value of Planck constant $h_{\text{eff}} = n \times h$.

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